

# Seung-Yeon Ryoo

## Curriculum Vitae

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### Employment

- **Olga Taussky and John Todd Postdoctoral Scholar Teaching Fellow in Mathematics** Aug 2023 - current  
Division of Physics, Mathematics and Astronomy, California Institute of Technology, Pasadena, USA  
- Postdoctoral Mentor: Thomas Hutchcroft

### Education

- **Ph. D. in Mathematics.** Sep 2018 - May 2023  
Princeton University, New Jersey, USA  
- Thesis advisor: Assaf Naor  
- Thesis title: "On the sharpness of the Assouad embedding theorem for finitely generated groups of polynomial growth and nilpotent Lie groups", available at Proquest.
- **B. Sc. in Mathematics.** Mar 2012 - Feb 2018  
Seoul National University, Seoul, Korea  
- Graduated *Summa Cum Laude* in 2018. GPA 4.26/4.3.

### Research Interests

- Bi-Lipschitz and snowflake embeddings of metric spaces into Banach spaces.
- Poincaré inequalities on metric spaces.
- Analysis of mathematical models of synchronization.

### Publications

- [17] On oscillator death in the Winfree model I: the one-dimensional case. Preprint available at <https://arxiv.org/abs/2601.01203>
- [16] Inertia perturbation theory for the inertial Kuramoto model (with Hangjun Cho, Jiu-Gang Dong, and Seung-Yeal Ha). Preprint available at <https://arxiv.org/abs/2508.11241>
- [15] Quantitative relaxation dynamics from generic initial configuration in the inertial Kuramoto model (with Hangjun Cho, Jiu-Gang Dong, and Seung-Yeal Ha). Preprint available at <https://arxiv.org/abs/2503.00720>
- [14] Asymptotics of Riemannian Lie groups with nilpotency step 2 (with Enrico Le Donne, Sebastiano Nicolussi Golo, and Luca Nalon). Preprint available at <https://arxiv.org/abs/2503.00560>
- [13] Quantitative nonembeddability of groups of polynomial growth into uniformly convex spaces. Preprint available at <https://arxiv.org/abs/2207.11305>.
- [12] Asymptotic formation and orbital stability of phase-locked states in Kuramoto–Lohe type synchronization models on Lie groups. *Commun. Math. Sci.* **23** 1221–1239 (2025). <https://dx.doi.org/10.4310/CMS.250517000730>
- [11] Embedding snowflakes of Carnot groups into bounded dimensional Euclidean spaces with optimal distortion. *Analysis & PDE.* **15** 1933–1990 (2022). <https://doi.org/10.2140/apde.2022.15.1933>
- [10] Constants of motion for the Lohe model with frustration and its applications to emergent dynamics (with Seung-Yeal Ha, Dohyun Kim and Hansol Park). *Physica D: Nonlinear Phenomena.* **416**, 132781 (2021). <https://doi.org/10.1016/j.physd.2020.132781>

- [9] Asymptotic phase-locking dynamics and critical coupling strength for the Kuramoto model (with Seung-Yeal Ha). *Commun. Math. Phys.* **377** 811-857 (2020). <https://doi.org/10.1007/s00220-020-03786-1>
- [8] On the relaxation dynamics of Lohe oscillators on some Riemannian manifolds (with Seung-Yeal Ha, Dongnam Ko). *J. Stat. Phys.* **172** 1427-1478 (2018) <https://doi.org/10.1007/s10955-018-2091-0>
- [7] Emergence of partial locking states from the ensemble of Winfree oscillators (with Seung-Yeal Ha, Dongnam Ko, Jinyeong Park). *Quart. Appl. Math.* **75** 39-68 (2017) <https://doi.org/10.1090/qam/1448>
- [6] Emergent dynamics of a generalized Lohe model on some class of Lie groups (with Seung-Yeal Ha, Dongnam Ko). *J. Stat. Phys.* **168** 171-207 (2017) <https://doi.org/10.1007/s10955-017-1797-8>
- [5] On the finiteness of collisions and phase-locked states for the Kuramoto model (with Seung-Yeal Ha, Hwa Kil Kim). *J. Stat. Phys.* **163**, 1394-1424 (2016) <https://doi.org/10.1007/s10955-016-1528-6>
- [4] Emergence of phase-locked states for the Kuramoto model in a large coupling regime (with Seung-Yeal Ha, Hwa Kil Kim). *Commun. Math. Sci.* **14** 1073-1091 (2016) <http://dx.doi.org/10.4310/CMS.2016.v14.n4.a10>
- [3] On the emergence and orbital stability of phase-locked states for the Lohe model (with Seung-Yeal Ha). *J. Stat. Phys.* **163**, 411-439 (2016) <https://doi.org/10.1007/s10955-016-1481-4>
- [2] Emergent dynamics of Winfree oscillators on locally coupled networks (with Seung-Yeal Ha, Dongnam Ko, Jinyeong Park). *J. Differential Equations* **260**, 4203-4236 (2016) <https://doi.org/10.1016/j.jde.2015.11.008>
- [1] Emergence of phase-locked states for the Winfree model in a large coupling regime (with Seung-Yeal Ha, Jinyeong Park). *Discrete and Continuous Dynamical Systems* **35**, 3417-3436 (2015) <http://dx.doi.org/10.3934/dcds.2015.35.3417>

## Teaching and Grading

- **Instructor at Caltech**

- Ma 109a, Introduction to Geometry and Topology, Fall 2025 (Rating: 4.65/5, Department average: 4.32/5)
- Ma 109c, Introduction to Geometry and Topology, Spring 2025 (Rating: 4.66/5, Department average: 4.44/5)
- Ma 157c, Topics in Geometry and Topology, Spring 2025 (Rating: 4.63/5, Department average: 4.44/5)
- Ma 191a, Selected Topics in Mathematics: Low-Dimensional Embeddings of Doubling Metrics, Fall 2024 (Rating: 4.62/5, Department average: 4.25/5)
- Ma 109c, Introduction to Geometry and Topology, Spring 2024 (Rating: 4.65/5, Department average: 4.25/5)
- Ma 157b, Riemannian Geometry, Spring 2024 (Rating: 4.92/5, Department average: 4.25/5)

- **Teaching Assistant at Princeton University**

- MAT 325, Analysis I: Fourier Analysis and Partial Differential Equations, Spring 2023 (grader)
- MAT 335, Analysis II: Complex Analysis, Fall 2022 (preceptor)
- MAT 325, Analysis I: Fourier Analysis and Partial Differential Equations, Spring 2022 (grader)
- MAT 425, Analysis III: Integration Theory and Hilbert Spaces, Fall 2021 (grader)
- MAT 325, Analysis I: Fourier Analysis and Partial Differential Equations, Spring 2021 (grader)
- MAT 335, Analysis II: Complex Analysis, Fall 2020 (preceptor)
- MAT 325, Analysis I: Fourier Analysis and Partial Differential Equations, Spring 2020 (grader)
- MAT 335, Analysis II: Complex Analysis, Fall 2019 (preceptor)

## Seminar/Conference Organization

- **Metric Embeddings**

Jul 2025

- Co-organizers: Alexandros Eskenazis (Sorbonne Univ., Univ. of Cambridge), Assaf Naor (Princeton Univ.)
- Location: American Institute of Mathematics, Pasadena, California, USA.
- Homepage: <https://aimath.org/pastworkshops/metricembeddings.html>

- **Graduate Student Seminar** Sep 2019 - May 2020  
Co-organizer: Vikram Giri (Princeton Univ.)  
Location: Princeton University, Princeton, New Jersey, USA.
- **Workshop for Students in Analysis and PDE** Jul 2018  
Co-organizers: Hyunseok Kim (Sogang Univ.), Hyunwoo Kwon (Sogang Univ), Young-Ran Lee (Sogang Univ.)  
Location: Sogang University, Seoul, Korea.  
Homepage: <https://sites.google.com/view/wsap2018>

## Honors, Awards, and Fellowships

- **AMS-Simons Travel Grant** Jul 2023  
American Mathematical Society, Simons Foundation
- **Overseas PhD Scholarship** Sep 2018 - Jun 2023  
Korea Foundation for Advanced Studies
- **Centennial Fellowship in the Natural Sciences and Engineering** Sep 2018 - Jun 2022  
Princeton University
- **Grand Prize - 35th University Students' Contest of Mathematics** Dec 2016  
Korean Mathematical Society
- **Undergraduate Scholarship** Sep 2015 - Feb 2018  
Korea Foundation for Advanced Studies
- **Gold Medal, Best Individual Award - 5th International Earth Science Olympiad** Sep 2011  
International Geoscience Education Organization

## Referee Work

- Communications in Mathematical Sciences, Dynamical Systems, Journal of Global Optimization, Journal of Statistical Physics, and Nonlinearity.

## Outreach

- Organizer for the Gender minorities and Women in Physics, Mathematics and Astronomy program at Caltech 2024-2025
- Diversity Co-Chair of the Caltech Postdoctoral Association 2024-2025

## Student Mentored

- Grace To Summer 2025  
Caltech Summer Undergraduate Research Fellowship

## Membership in Professional Societies

- American Mathematical Society (AMS)
- Society for Industrial and Applied Mathematics (SIAM)
- Korean Mathematical Society (KMS)

## Invited Talks and Visiting Positions

- **A conjectural low-dimensional embedding of doubling metric spaces** Nov 2025  
Functional Analysis in the Pacific Northwest, University of Oregon, Oregon, USA.
- **Group embeddings and coarse differentiation** Oct 2025  
Spectral Gaps, Isaac Newton Institute for Mathematical Sciences, London, UK.

• <b>Sharpening the Assouad embedding theorem</b>	Oct 2025
AMS Fall Southeastern Sectional Meeting, Tulane University, New Orleans, USA.	
• <b>Asymptotics of Riemannian Lie groups with nilpotency step 2</b>	Aug 2025
2025 2K-GATE One day Geometric Topology Festival, Korea Institute for Advanced Studies, Seoul, Korea	
• <b>Sharpening the Assouad embedding theorem</b>	Aug 2025
Virtual Seminar on Geometry and Topology, Korea Institute for Advanced Studies, Seoul, Korea	
• <b>Visiting Researcher</b>	Aug-Sep 2025
Korea Institute for Advanced Studies, Seoul, Korea	
• <b>Embedding via heat kernels</b>	Jun 2025
CRM-PIMS Summer School in Probability, University of British Columbia, Vancouver, British Columbia, Canada.	
• <b>Towards a sharp form of the Assouad embedding theorem</b>	Mar 2025
Ohio River Analysis Meeting, University of Cincinnati, Cincinnati, Ohio, USA.	
• <b>Quantitative nonembeddability of nilpotent groups into uniformly convex spaces</b>	Mar 2025
Winter School on Geometric Analysis, Geilo, Norway.	
• <b>Lipschitz Padded Nested Random Partitions</b>	Oct 2024
20th Prairie Analysis Seminar, University of Kansas, Lawrence, Kansas, USA.	
• <b>Lipschitz Padded Nested Random Partitions</b>	Jul 2024
Analysis Seminar, Korea Institute for Advanced Studies, Seoul, Korea.	
• <b>Quantitative nonembeddability of nilpotent groups into uniformly convex spaces</b>	Nov 2023
University of Cincinnati Analysis Seminar, Cincinnati, Ohio, USA.	
• <b>Improving Assouad's theorem on nilpotent groups</b>	Nov 2023
19th Prairie Analysis Seminar, Manhattan, Kansas, USA.	
• <b>Dorronsoro's theorem and vertical-versus-horizontal inequalities on Carnot groups</b>	Aug 2023
AWM-MAA Invited Paper Session on Geometric Measure Theory, Harmonic Analysis, and Partial Differential Equations, Tampa, Florida, USA.	
• <b>Embedding finitely generated groups of polynomial growth into Euclidean space</b>	Jul 2023
Virtual Seminar on Geometry and Topology, Korea Institute for Advanced Studies, Seoul, Korea.	
• <b>Visiting Researcher</b>	Jul 2023
Korea Institute for Advanced Studies, Seoul, Korea	
• <b>Embedding balls in groups of polynomial growth into Euclidean space</b>	Jun 2023
Sub-Riemannian Geometry and Beyond III, Centro De Giorgi, Pisa, Italy.	
• <b>On embedding finitely generated groups of polynomial growth into Euclidean spaces</b>	Apr 2023
Analysis and PDE Seminar, University of California, Los Angeles, Los Angeles, USA.	
• <b>On embedding finitely generated groups of polynomial growth and nilpotent Lie groups into uniformly convex spaces</b>	Dec 2022
Geometry and Geometric Analysis Working Group, New York University, New York, USA.	
• <b>The correct exponent for the Gotsman–Linial conjecture, after D. Kane</b>	Oct 2022
Computational Learning Theory and Fourier Analysis, online.	
• <b>Vertical versus horizontal inequalities on nilpotent Lie groups and groups of polynomial growth</b>	Aug 2022
Dynamics seminar, Seoul National University, Seoul, Korea.	

- **Vertical versus horizontal inequalities on nilpotent Lie groups and groups of polynomial growth** Aug 2022  
Virtual Seminar on Geometry and Topology, Korea Institute for Advanced Studies, Seoul, Korea.
- **Vertical versus horizontal inequalities on nilpotent Lie groups and groups of polynomial growth** Aug 2022  
Concentration Week on Geometry and Analysis on Nonsmooth Spaces, Texas A&M University, Texas, USA.
- **A sharp form of the Assouad embedding theorem for Carnot groups** Aug 2022  
Graduate Concentration Week on Metric Geometry, Texas A&M University, Texas, USA.
- **Two mathematical models of synchronization** Apr 2022  
Program in Applied and Computational Sciences Graduate Student Seminar, Princeton University, New Jersey, USA.
- **Vertical versus horizontal inequalities on Carnot groups via a Dorronsoro theorem and Littlewood–Paley–Stein theory** Mar 2022  
AMS Spring Central Virtual Sectional Meeting, Purdue University, Indiana, USA.
- **Dorronsoro's theorem and vertical versus horizontal Poincaré inequalities on Carnot groups** Jan 2022  
Workshop for Young Mathematicians in Korea, Seoul, Korea.
- **Talagrand's influence inequality revisited, after D. Cordero-Erausquin and A. Eskenazis** Oct 2021  
Discrete Analysis and Complexity of Quantum Algorithms, online.
- **A sharp form of Assouad's embedding theorem for Carnot groups** May 2021  
Online Asymptotic Geometric Analysis Seminar, online.
- **A sharp form of Assouad's embedding theorem for Carnot groups** Mar 2021  
AMS Spring Eastern Virtual Sectional Meeting, Brown University, Rhode Island, USA.
- **Embedding snowflakes of Carnot groups into bounded dimensional Euclidean spaces with optimal distortion** Aug 2020  
HYKE-Hwarang Invited Talk, Seoul National University, Seoul, Korea.
- **Embedding metric spaces into  $\ell^p$**  Feb 2020  
Undergraduate (“Nullset”) colloquium, Princeton University, New Jersey, USA.
- **Krivine's theorem and related results** Apr 2019  
Graduate Student Seminar, Princeton University, New Jersey, USA.
- **Recent developments in the Assouad embedding theorem** Dec 2018  
Graduate Student Seminar, Sogang University, Seoul, Korea.
- **On the Critical Coupling Strength of the Kuramoto model** Jul 2018  
Workshop for students in Analysis and PDE, Sogang University, Seoul, Korea.
- **Emergent dynamics of a generalized Lohe model on some class of Lie groups** Aug 2017  
Intercollegiate Undergraduate (“Stupid Mathematics”) Seminar, Sogang University, Seoul, Korea.
- **The Kuramoto model: a paradigm for synchronization** Aug 2016  
Intercollegiate Undergraduate (“Stupid Mathematics”) Seminar, Sogang University, Seoul, Korea.

## Other Experience

- **Military Service** Sep 2013 - Sep 2015  
Republic of Korea Air Force