



# Inferring Strategic Voting Kawai and Watanabe(2011)

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# Outline

- Introduction
- Model
- Data
- Empirical Analysis
- Results and Counterfactual Experiment
- Conclusion

# Introduction

## **Main question solved in this paper:**

- Can we identify the existence and fraction of strategic voters?

## **Empirical methodologies used in the past studies:**

- Aggregate regression
- Self-reporting survey
- Direct measurement
- Laboratory Experiment

# Introduction

## Definition

- Sincere voting: voting according to preferences
- Strategic voting: voting conditioning on pivotality
- Misaligned voting: voting for a candidate other than the most-preferred
- Pivotality: the state of having the decisive vote

**the set of misaligned voters is only a subset of the set of strategic voters.**

# Model

## Environment:

- Plural-rule election
- $K$  candidates for one seat in one district
- $M$  municipalities in an electoral district

## Voter's utility function

$$u_{nk} = u(x_n, z_k) + \xi_{km} + \varepsilon_{nk}$$

- $x_n$  :Voter  $n$ 's characteristic
- $z_k$  :Candidate  $k$ 's characteristics
- $\xi_{km}$  :Candidate  $k$ 's shock on municipality  $m$
- $\varepsilon_{nk}$  :Voter  $n$ 's preference shock

# Model

## Voter's strategies:

- Sincere: vote for candidate  $k$  IFF  $u_{nk} \geq u_{nl} \forall l$
- Strategic: vote for candidate  $k$  IFF  $\overline{u_{nk}}(T_n) \geq \overline{u_{nl}}(T_n) \forall l$

## Expected utility from voting for candidate $k$ :

$$\overline{u_{nk}}(T_n) = \frac{1}{2} \sum_{l \in \{1..K\}} T_{n,kl} (u_{nk} - u_{nl})$$

- $T_{n,kl}$  : Voter  $n$  's belief that his vote would be pivotal: belief that candidate  $k$  and  $l$  would be tied for the first place or that  $k$  will be one vote behind.

# Model

## Further assumptions

- Beliefs are common across all voters in the same district (Beliefs over tie probabilities are common across the same district)
- Denote the type of voter  $n$  in municipality  $m$  by a random variable:

$$\alpha_{nm} = \begin{cases} 0 & \text{if voter } n \text{ is sincere} \\ 1 & \text{if voter } n \text{ is strategic} \end{cases}$$

- The probability that voter  $n$  in municipality  $m$  is a strategic voter( $\alpha_m$ ) is drawn iid from a conditional distribution  $F_\alpha(\cdot | w)$  where  $w$  reflects the closeness based on election forecasts.

# Model

## Aggregating vote share:

$$V_{k,m}^{SIN} = \frac{\sum_{n=1}^{N_m} (1 - \alpha_{nm}) \cdot 1\{u_{nk} \geq u_{nl}, \forall l\}}{\sum_{n=1}^{N_m} (1 - \alpha_{nm})}$$

$$V_{k,m}^{SIR}(T) = \frac{\sum_{n=1}^{N_m} \alpha_{nm} \cdot 1\{\overline{u_{nk}} \geq \overline{u_{lk}}, \forall l\}}{\sum_{n=1}^{N_m} \alpha_{nm}}$$

$$V_{k,m}(T) = \frac{\sum_{n=1}^{N_m} \alpha_{nm} \cdot V_{k,m}^{SIR}(T)}{N_m} + \frac{\sum_{n=1}^{N_m} (1 - \alpha_{nm}) \cdot V_{k,m}^{SIN}(T)}{N_m}$$



# Data

## General information

- Source: Japanese House Representatives election
- Vote share and candidate characteristics (*from ATES*)
- Demographic information(*from Social and Demographic Statistics of Japan*)
- Data selection criteria:
  - 3 or 4 candidates
  - No recent mergers
  - Minimum of 2 municipalities

# Data

	mean	st. dev.	min	max	# obs
# of municipalities per district	9.23	7.27	2	36	159
3-candidate district	8.72	7.03	2	36	144
4-candidate district	14.13	8.02	3	36	15
winner's vote share (%)	51.72	6.83	28.98	73.62	159
3-candidate district	52.90	5.70	36.03	73.62	144
4-candidate district	40.46	6.69	28.98	55.89	15
winning margin (%)	13.53	10.23	0.06	53.92	159
3-candidate district	14.05	10.17	0.17	53.92	144
4-candidate district	8.50	9.73	0.06	35.50	15
margin between 2nd and 3rd (%)	28.51	9.67	0.00	43.32	159
3-candidate district	30.39	7.65	0.00	43.32	144
4-candidate district	10.45	8.51	0.57	23.32	15
pre-election forecast on closeness	2.33	0.81	1	4	159
3-candidate district	2.36	0.82	1	4	144
4-candidate district	2.07	0.59	1.5	3.5	15

# Data

vote share – JCP	7.62	2.72	2.77	17.02	154
vote share – DPJ	38.56	8.80	10.78	60.10	159
vote share – LDP	49.66	8.90	23.19	73.62	159
vote share – YUS	34.95	9.10	14.50	49.58	20
ideology – JCP	1.97	0.36	1	2.75	154
ideology – DPJ	3.10	0.60	1	4.50	159
ideology – LDP	3.12	0.61	1.25	4.67	159
ideology – YUS	2.55	0.45	1.25	3.25	20

**The situation might be very different in 4-candidate districts:**

- Voters may have beliefs in **three way ties** rather than **two-way ties**.
- Since the prediction would be very **ambiguous** in a 4-candidate district, the common belief might be violated.

# Empirical Analysis

## Specification of the model

$$u_{nk} = u(x_n, z_k, \theta^{PREF}) + \xi_{km} + \varepsilon_{nk} = -(\theta^{ID} x_n - \theta^{pos} z_k^{POS})^2 + \theta^{QLTY} z_{km}^{QLTY} + \xi_{km} + \varepsilon_{nk}$$

**voters' ideology is assumed to be a function of demographics**

- $x_n$  :voter characteristics
- $z_{km} = \{z_k^{POS}, z_{km}^{QLTY}\}$  :Candidate characteristics
  - $z_k^{POS}$  :Ideological characteristics
  - $z_{km}^{QLTY}$  :Non-ideological characteristics
- $\theta^{PREF}$  :vector of preference parameters

# Empirical analysis

## **Partial Identification of preference parameters**

- Two kinds of restrictions:

Restriction (I): voters do not vote for their least-preferred candidate

Restriction (II): common belief within one district.

- With two restrictions, the parameters can only be partially identified.

## **Partial Identification of the fraction of the strategic voters**

- Vary the identified set of  $\theta^{REF}$  to trace out the identified set of the parameters that determine the extent of strategic voting
- When there is a large number of strategic voters, the actual vote share can systematically diverge from the predicted outcome.

# Empirical analysis

## Parameters estimated

- $\theta^{PREF}$  :Preference parameters
- $(\theta_{\alpha 1}, \theta_{\alpha 2})$ :Parameters that determine the distribution of strategic voters

## Estimation steps

- For some district, regress the vote share data of candidate  $k$  in each municipality on the demographic data to obtain coefficients.
- Fix preference parameters, beliefs, fraction of strategic voters and municipality shocks; compute the simulated vote share.
- Regress the simulated vote share on demographic data to obtain regression coefficients.
- Vary beliefs to obtain minimum and maximum for the coefficients.
- Integrate out the fraction of strategic voters and municipality shocks
- Find out the moment inequality and apply Pakes, Porter, Ho, and Ishii(2007)



# Main Results

## Parameter estimates

Parameter	Confidence Interval
$\theta_1^{const}$	$[-0.556, -0.543]$
$\theta_1^{income}$	$[-0.028, -0.025]$
$\theta_1^{education}$	$[-0.109, -0.104]$
$\theta_1^{above65}$	$[0.136, 0.141]$
$\theta^{YUS}$	$[-0.701, -0.695]$
$\theta^{JCP}$	$[-2.495, -2.482]$
$\theta^{DPJ}$	$[-1.975, -1.969]$
$\theta_2^{const}$	$[2.629, 2.635]$
$\theta_2^{income}$	$[-0.637, -0.625]$
$\theta_2^{education}$	$[0.339, 0.349]$
$\theta_2^{above65}$	$[-0.056, -0.052]$

Voters with lower income, fewer years of schooling prefer LDP, YUS.

Voters with **lower** income, **longer** years of schooling prefer pro-market candidates

ideology – JCP	1.97	0.36	1	2.75	154
ideology – DPJ	3.10	0.60	1	4.50	159
ideology – LDP	3.12	0.61	1.25	4.67	159
ideology – YUS	2.55	0.45	1.25	3.25	20

# Main Results

## **The fraction of strategic voters and misaligned voters**

- The authors estimate the fraction of strategic voters to be [63.4% , 84.9%]
- The authors determine the fraction of misaligned voters to be [1.4%, 4.2%]

## **Counterfactual Experiment: Sincere voting under plurality rule**

- The change in vote share is small (due to a small fraction of misaligned voter)
- Change in the number of seats is considerable (due to small winning margin)



# Conclusion

- **The authors find a much larger fraction of strategic voters than in the past studies.**
- **The authors consider including abstention in the future method.**
- **My suggestions:**
  - Drop the sample of 4-candidate districts and go through the estimation again to see if there is a big difference.
  - Find more accurate indicators for individual ideologies. (i.e data from local surveys)