

queueing & scheduling

- consider a cell switch with N inputs & N outputs with identical link (line) rates
- assume cell arrivals occur at the beginning of a slot & cell departures are completed by the end of the slot
- a switch can be input-queued (IQ), output-queued (OQ) or combined input-output-queued (CIOQ)
- let p be the maximum no. of packets that can be switched by the fabric in 1 slot, & let q be the maximum no. of packets that can be switched to an output in 1 slot
 - if $p < N$, input queueing is needed
 - if $q > 1$, output queueing is needed
- we can achieve $p, q > 1$ by operating the switching fabric at a rate higher than the line rate, i.e. a speedup of the fabric (time-based), or parallelism in the fabric (space-based), or a combination of both
- the placement of the queues, the buffer sizes of the queues, & the switch fabric & memory speeds are important design parameters

OQ switch

- should operate at N times the line rate & have an output queue memory transfer rate of $N+1$ times the line rate (in the worst case, N cells are transferred from the N inputs to an output & one of them is transmitted on the output link in 1 slot)
- work-conserving (no output link is idle if there is a cell meant for that output in the switch), easy to do QoS scheduling, eg WFQ

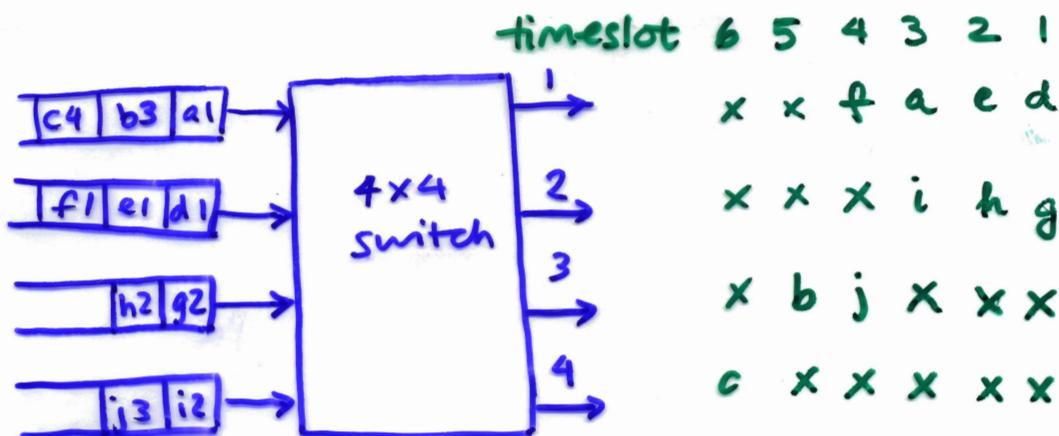
IQ switch

- if there is contention for some output, only 1 cell is switched to that output in the slot
- can be operated at the line rate (i.e. each input sends at most 1 cell & each output receives at most 1 cell in a slot) with a memory transfer rate twice the line rate (i.e. 1 cell can be written to & read from each queue in a slot)
- if each input has a FIFO queue, head-of-line (HOL) blocking occurs if more than 1 HOL cell from the input queues has the same destination — so all but 1 of them remain in their queues — and one of these queues contains a non-HOL cell whose

destination is free — this cell is not switched and its destination is idle during the slot
 → the IQ switch with FIFO queuing is not work-conserving

Eg.

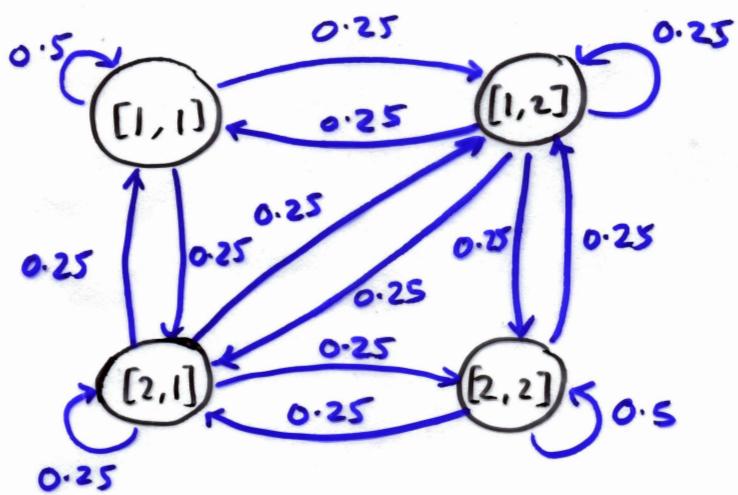
inputs



(input cells are labelled with a letter ID & a no. indicating the destination part of the cell)

(output cell departures in each timeslot — 'x' indicates no transmission)

- the loss in throughput relative to the OQ switch tends to grow with switch size
- consider the case of saturated inputs for an $N \times N$ IQ switch with FIFO queuing
- assume each cell's destination is chosen independently & uniformly at random over the N outputs, & that if there is output contention, one of the cells is chosen randomly to be switched
- consider the case $N=2$, & let $d_n^{(i)}$ denote the destination of input i 's HOL cell in slot n
- $d_n \triangleq [d_n^{(1)} \ d_n^{(2)}]$ evolves according to a Markov chain



- the stationary probability of the switch being in each of the 4 states is 0.25
- if $d_n = [1,1]$ or $[2,2]$, only 1 cell is switched in slot n , & the throughput is 0.5 cells per port; if $d_n = [1,2]$ or $[2,1]$, both cells are switched in slot n , & the throughput is 1 cell per port
 → the stationary saturation throughput of the switch is thus 0.75 cells per port
- for $N \rightarrow \infty$, the saturation throughput can be shown to converge to $2 - \sqrt{2} \approx 0.586$ cells per port
- the 1Q switch with FIFO queuing operated at line rate & the 0Q switch are at 2 ends of a tradeoff between throughput & resources/complexity
- the line-rate 1Q switch can be improved w non-FIFO queuing, e.g.
 - windowing : the scheduler can select 1 of the first w cells from each input queue (vs HOL blocking)
 - virtual output queuing : each input maintains a separate queue for each output (eliminates HOL blocking) & the scheduler chooses a matching

between inputs & outputs (because of line-rate switching constraint)

- ideal throughput (i.e. queues are stable for any feasible arrival rates where the desired rate for each input & output is ≤ 1 cell / timeslot) is achieved with maximum weight matching, where the weight w_{ij} for the edge from input i to output j is given by either
 - the length of the queue Q_{ij} for output j at input i , or
 - the no. of slots that the oldest cell in Q_{ij} has waited
- practical switches use suboptimal matching algorithms which are less complex

C10Q switch

- up to L cells, $1 < L < N$, can be switched to an output in 1 slot
- saturation throughput for $N \rightarrow \infty$ can be very close to 1 even for small L (exact performance depends on details of the input scheduler, etc)
- a C10Q switch can be used to emulate an OQ switch with QoS scheduling, but this utilizes a relatively complex centralized scheduler